

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				

Pearson Edexcel International Advanced Level

Monday 28 October 2024

Morning (Time: 1 hour 30 minutes) **Paper reference** **WMA14/01**

Mathematics

International Advanced Level

Pure Mathematics P4

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 10 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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1. (a) Find the first 4 terms of the binomial expansion, in ascending powers of x , of

$$(8 - 3x)^{-\frac{1}{3}} \quad |x| < \frac{8}{3}$$

giving each coefficient as a simplified fraction.

(4)

- (b) Use the answer from part (a) with $x = \frac{2}{3}$ to find a rational approximation to $\sqrt[3]{6}$

(2)

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2.

**In this question you must show all stages of your working.
Solutions relying on calculator technology are not acceptable.**

The curve C_1 has equation

$$y = x^4 + 10x^2 + 8 \quad x \in \mathbb{R}$$

The curve C_2 has equation

$$y = 2x^2 - 7 \quad x \in \mathbb{R}$$

Use algebra to prove by contradiction that C_1 and C_2 do **not** intersect.

(4)

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3.

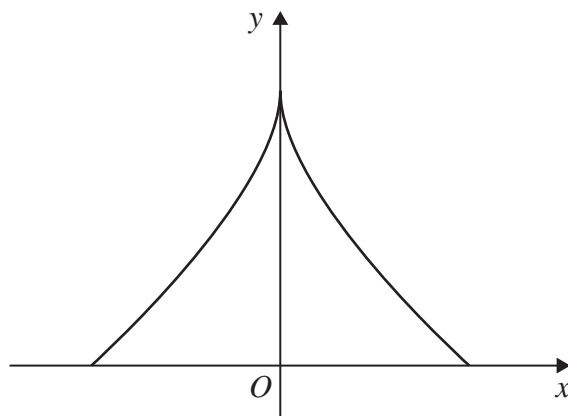


Figure 1

Figure 1 shows a sketch of the curve C with parametric equations

$$x = 3 \sin^3 \theta \quad y = 1 + \cos 2\theta \quad -\frac{\pi}{2} \leq \theta \leq \frac{\pi}{2}$$

(a) Show that

$$\frac{dy}{dx} = k \operatorname{cosec} \theta \quad \theta \neq 0$$

where k is a constant to be found.

(3)

The point P lies on C where $\theta = \frac{\pi}{6}$

(b) Find the equation of the tangent to C at P , giving your answer in the form $ax + by + c = 0$ where a , b and c are integers.

(3)

(c) Show that C has Cartesian equation

$$8x^2 = 9(2 - y)^3 \quad -q \leq x \leq q$$

where q is a constant to be found.

(3)



6. Use the substitution $u = \sqrt{x^3 + 1}$ to show that

$$\int \frac{9x^5}{\sqrt{x^3 + 1}} dx = 2(x^3 + 1)^k (x^3 - A) + c$$

where k and A are constants to be found and c is an arbitrary constant.

(5)

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7.

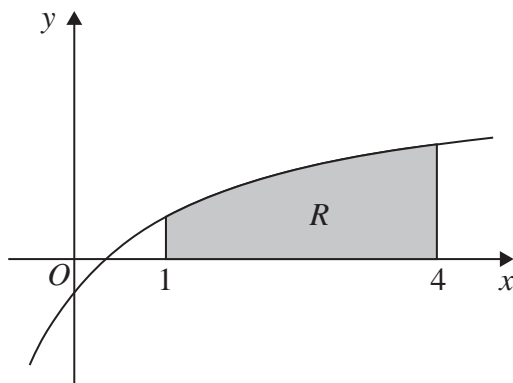


Figure 4

Figure 4 shows a sketch of part of the curve with equation

$$y = \frac{3x - 1}{x + 2} \quad x > -2$$

(a) Show that

$$\frac{3x - 1}{x + 2} \equiv A + \frac{B}{x + 2}$$

where A and B are constants to be found.

(2)

The finite region R , shown shaded in Figure 4, is bounded by the curve, the line with equation $x = 4$, the x -axis and the line with equation $x = 1$

This region is rotated through 2π radians about the x -axis to form a solid of revolution.

(b) Use the answer to part (a) and algebraic integration to find the exact volume of the solid generated, giving your answer in the form

$$\pi(p + q \ln 2)$$

where p and q are rational constants.

(6)



